

# THE MORSE-BOTT INEQUALITIES VIA DYNAMICAL SYSTEMS: ERRATUM CONCERNING THE ORIENTATION ASSUMPTIONS

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## Correction

The statement of Theorem 8 (Morse-Bott inequalities) in the paper says, “...assume that all of the critical submanifolds of  $f$  are orientable.” This should be corrected to, “...assume that all of the negative normal bundles of the critical submanifolds of  $f$  are orientable.”

## Discussion

If  $f : M \rightarrow \mathbb{R}$  is a Morse-Bott function, then the tangent bundle of  $M$  along a critical submanifold  $C \subseteq M$  splits as

$$T_*M = T_*C \oplus \nu_*^- C \oplus \nu_*^+ C$$

(see Lemma 5 of the paper), where  $\nu_*^- C$  is the negative normal bundle of  $C$ . In the paper it is assumed that  $M$  is orientable in order to simplify the exposition. However, even if  $T_*M$  is orientable, the assumption that  $T_*C$  is orientable is different from the assumption that  $\nu_*^- C$  is orientable, unless  $\nu_*^+ C$  is orientable.

The corrected orientation assumption is needed in the proof of Lemma 9 of the paper. In the statement of that lemma, the phrase “ $C_j$  is orientable” should be corrected to “ $\nu_*^- C_j$  is orientable”.

## Acknowledgments

We would like to thank Thomas Rot for pointing out the mistake in the orientation assumptions printed in the paper and providing a nice counterexample of a Morse-Bott function on  $\mathbb{R}P^5$  with two isolated critical points and a critical submanifold diffeomorphic to  $\mathbb{R}P^3$ .

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